

Commonly Used Distributions

The following table gives commonly used families of probability models.

Distribution Density

$$\text{Bern}(\theta) \quad f(y|\theta) = \theta^y(1 - \theta)^{1-y}$$

$$\text{Bin}(n, \theta) \quad f(y|\theta) = \binom{n}{y} \theta^y (1 - \theta)^{n-y}$$

$$\text{Beta}(a, b) \quad p(\theta) = \frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} \theta^{a-1} (1-\theta)^{b-1} I_{(0,1)}(\theta)$$

$$U(0, 1) \quad p(\theta) = I_{(0,1)}(\theta)$$

$$\text{Pois}(\theta) \quad f(y|\theta) = \theta^y e^{-y} / y!$$

$$\text{Exp}(\theta) \quad f(y|\theta) = \theta e^{-\theta y} I_{(0,\infty)}(y)$$

$$\text{Gamma}(a, b) \quad p(\theta) = [b^a / \Gamma(a)] \theta^{a-1} e^{-b\theta} I_{(0,\infty)}(\theta)$$

$$\chi^2(n) \quad \text{Same as Gamma}(n/2, 1/2)$$

$$\text{Weib}(\alpha, \theta) \quad f(y|\theta) = \theta \alpha y^{\alpha-1} \exp(-\theta y^\alpha) I_{(0, \infty)}(\theta)$$

$$N(\theta, 1/\tau) \quad f(y|\theta, \tau) = (1/\sqrt{2\pi\tau}) \exp[-\tau(y - \theta)^2/2]$$

$$t(n, \theta, \sigma) \quad f(y|\theta) = \left[1 + (y - \theta)^2/n\sigma^2\right]^{(n+1)/2}$$

$$\times \Gamma[(n + 1)/2]/\Gamma(n/2)\sigma\sqrt{n\pi}$$

$$\text{Cauchy}(\theta) \quad \text{same as } t(1, \theta, 1)$$

$$\text{Dirichlet}(a_1, a_2, a_3) \quad p(\theta) = \frac{\Gamma(a_1+a_2+a_3)}{\Gamma(a_1)\Gamma(a_2)\Gamma(a_3)}$$

$$\times \theta_1^{a_1-1} \theta_2^{a_2-1} (1 - \theta_1 - \theta_2)^{a_3-1}$$

$$\times I_{(0,1)}(\theta_1) I_{(0,1)}(\theta_2) I_{(0,1)}(1 - \theta_1 - \theta_2)$$